

7 A particle moves in a straight line so that, t s after passing through a fixed point O , its velocity, v ms⁻¹, is given by $v = \frac{60}{(3t + 4)^2}$.

For
Examiner's
Use

(i) Find the velocity of the particle as it passes through O . [1]

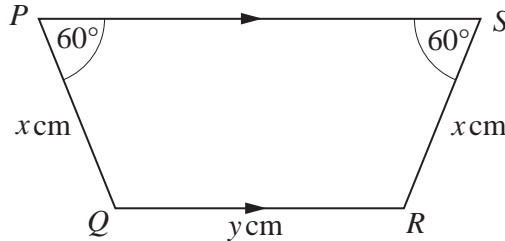
(ii) Find the acceleration of the particle when $t = 2$. [3]

(iii) Find an expression for the displacement of the particle from O , t s after it has passed through O . [4]

11 Answer only **one** of the following two alternatives.

EITHER

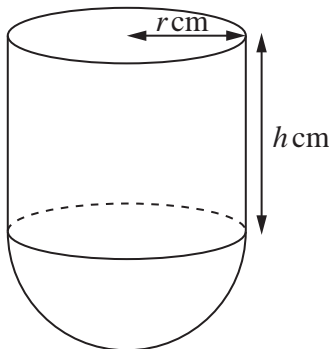
- (a) Using an equilateral triangle of side 2 units, find the exact value of $\sin 60^\circ$ and of $\cos 60^\circ$. [3]
- (b)



$PQRS$ is a trapezium in which $PQ = RS = x$ cm and $QR = y$ cm.
Angle $QPS =$ angle $RSP = 60^\circ$ and QR is parallel to PS .

- (i) Given that the perimeter of the trapezium is 60 cm, express y in terms of x . [2]
- (ii) Given that the area of the trapezium is A cm², show that
- $$A = \frac{\sqrt{3}(30x - x^2)}{2}. \quad [3]$$
- (iii) Given that x can vary, find the value of x for which A has a stationary value and determine the nature of this stationary value. [4]

OR



For a sphere of radius r :

$$\text{Volume} = \frac{4}{3}\pi r^3$$

$$\text{Surface area} = 4\pi r^2$$

The diagram shows a solid object in the form of a cylinder of height h cm and radius r cm on top of a hemisphere of radius r cm. Given that the volume of the object is 2880π cm³,

- (i) express h in terms of r , [2]
- (ii) show that the external surface area, A cm², of the object is given by
- $$A = \frac{5}{3}\pi r^2 + \frac{5760\pi}{r}. \quad [3]$$

Given that r can vary,

- (iii) find the value of r for which A has a stationary value, [4]
- (iv) find this stationary value of A , leaving your answer in terms of π , [2]
- (v) determine the nature of this stationary value. [1]